

## Simulation of Internal Ballistics Solid Rocket Motor

MAGDI ABELRAZIG ELHAG MOHAMED

School of Mechanical Engineering

Sudan University of Science & Technology, Khartoum, Sudan

MOHAMED ELTAYEB MANSOUR

Associate Professor, Aviation Department

Karary University, Khartoum, Sudan

### Abstract:

*Determination of the grain geometry is one of the critical steps during the design of a solid propellant rocket motor. Because, performance prediction of the solid propellant rocket motor is achieved if burning surface area of the propellant grain is known as it recedes.*

*Solid Rocket Motors (SRM) were very expensive. In the design to develop the solid propellant rocket motors, the use of numerical tools able to simulate, predict and reconstruct the behavior of a given motor in all its operative conditions is particularly important in order to decrease all the planning and costs to avoid made destructive test for checking internal ballistic which is very expensive.*

*The main goal of this work is to study and simulate charged motor for long range rocket (122mm) motor internal ballistics (thrust & pressure), during the quasi steady state by means of a commercial numerical tool, ANSYS FLUENT.*

*The internal ballistics model constructed in this study is a 2-D axis symmetric model, based on several assumptions. Among them is the assumption that there is no contribution of the erosive burning and the dynamic burning in the burning rate model.*

*The results of the internal ballistics simulation are compared with the results found in the experimental ground firing test station, thus validating the model that has been set up. The validation of the results also allows us to conclude that the assumptions made in the construction of the model are reasonable. Good agreement observed between experimental results and analytical and simulation results.*

*In this study some of the conventional two dimensional grain burn backs are analyzed and thrust - pressure time histories are predicted by making some graphs. These graphs are validated by comparing the ground static firing test data obtained by Ballistic Test Motor.*

*ANSYS FLUENT simulation can improved to use in investigating other solid rocket motors which used in missile or rockets motor or any other type of ammunitions which is too high cost to investigate with experimental ground firing test station.*

**Key words:** Thrust, ANSYS FLUENT, Pressure, solid propellant, Internal Ballistic, Solid Rocket Motor.

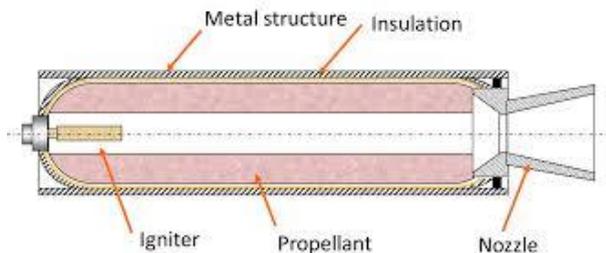
## **1. INTRODUCTION**

First part of the design process of the solid propellant rocket motor is the determination of the flight-mission requirements. After that, thrust-time curve is prepared according to requirements. At this point, internal ballistic calculations are performed to estimate chamber pressure of the rocket motor [1, 3, 4, 9].

Solid rockets motors (SRM) store propellants in solid form. It is the simplest of all rocket propulsion system designs .The fuel is typically powdered aluminum and the oxidizer is ammonium perchlorate. A synthetic rubber binder such as polybutadiene holds the fuel and oxidizer powders together. Though lower performing than liquid propellant rockets, the operational simplicity of a solid rocket motor often makes it the propulsion system of choice [2,4] .

The combustion mechanisms for solid rocket propellants are quite complex and dependent on many local fluid, chemical, and thermal phenomena. Many solid rocket propellant burning-rate models are greatly simplified because of limited computational power and understanding of the combustion process [2, 5].

A solid-propellant rocket motor consists of a casing, usually steel, filled with a solid propellant charge, called the grain, which contains all the chemical constituents (fuel plus oxidizer) for complete burning, the nozzle, internal insulation and the igniter, as shown in Figure 1.1. The combustion chamber is where the burning of propellants takes place at high pressure. The chamber must be strong enough to contain the high pressure generated by, and the high temperature resulting from, the combustion process. Because of the high temperature and heat transfer, the chamber and nozzle are usually cooled. The chamber must also be of sufficient length to ensure complete combustion before the gases enter the nozzle. When ignited, the propellant compounds burn rapidly, expelling hot gases from a nozzle to produce thrust. The propellant burns from the center out toward the sides of the casing. The shape of the center channel determines the rate and pattern of the burn, thus providing a means to control thrust. Unlike liquid-propellant engines, solid-propellant motors can't be shut down. Once ignited, they burn until all the propellant is exhausted[10].

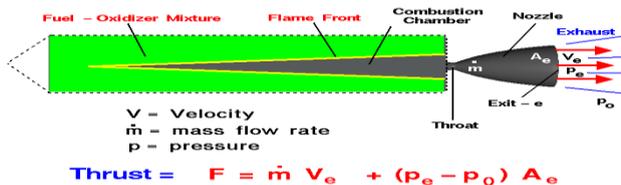


**Figure 1: Solid Rocket Motor (SRM)**

### **1.1 Thrust**

Thrust is a force or a push, also it is the force that propels a flying machine in the direction of motion .When a system pushes expels or accelerates mass in one direction, the accelerated mass will cause a force of equal magnitude but

opposite direction on that system. The force applied on a surface in a direction perpendicular or normal to the surface is called thrust. In math and physics, this is described by Isaac Newton's second and third laws. Thrust is used to describe how strongly an engine pushes [4].

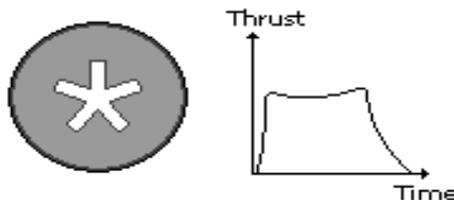


**Figure 2: Thrust variables & general thrust equation**

The thrust  $F$  is the resultant of the forces due to the pressures exerted on the inner and outer walls by the combustion gases and the surrounding atmosphere, taking the boundary between the inner and outer surfaces as the cross section of the exit of the nozzle.

### 1.2 Thrust-Time-Curve

A thrust curve, sometimes known as a "performance curve" or "thrust profile" is a graph of the thrust of an engine or motor, (usually a rocket) with respect to time. Most motors do not produce linear thrust (thrust which increases at a constant rate with time). Instead, they produce a curve of some type, where thrust will slowly rise to a peak, and then fall, or "tail off". Rocket engines, particularly solid-fuel rocket motors, produce very consistent thrust curves, making this a useful metric for judging their performance [5].



**Figure 3: Thrust - Time Curve**

### 1.3 Pressure.

Pressure is a force exerted by the substance per unit area on another substance. The pressure of a gas is the force that the gas exerts on the walls of its container. Pressure (symbol:  $p$  or  $P$ ) is the force applied perpendicular to the surface of an object per unit area over which that force is distributed.

Pressure is defined to be the amount of force exerted per area[1,3,4]..

$$P=F/A \quad (1)$$

### 1.4 Pressure-Time-Curve

Pressure time curve shows airway pressure, breath timing, the breath type delivered and patient versus machine triggering [2, 4, 5, 6, 7].

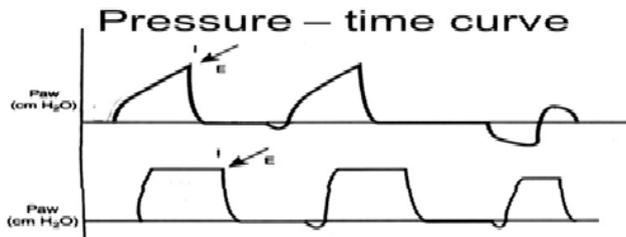
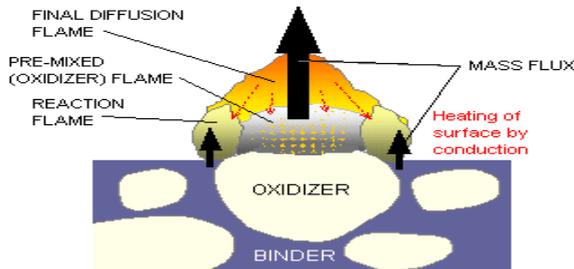


Figure 3: Pressure-Time Curve

### 1.5 Burning rate

The burn rate (or burning rate) in chemistry is a measure of the linear combustion rate of a compound or substance such as a candle or a solid propellant. It is measured in length over time, such as "mm/second" or "inches/second". Among the variables affecting burn rate are pressure and temperature. Burn rate is an important parameter especially in the area of propellants because it determines the rate at which exhaust gases are generated from the burning propellant which in turn decides the rate of flow through the nozzle. The thrust generated in the rocket of missile depends on this rate of flow. Thus knowing quantitatively the burning rate of a propellant, and how it

changes under various conditions, is of fundamental importance in the successful design of a solid rocket motor.



**Figure 4: Simplified model of propellant burning**

Burning rate is the principal ballistic property of a solid propellant, necessary for motor design and also used for control of propellant quality in production. The burning rate varies with pressure, and the rate-pressure relationship is most commonly determined by testing either strands or small motors at several different relatively constant pressures. [1, 4, 6, 11].

### **1.6 Vieille's - de Saint Robert's law:**

For SRM ignition transient modeling, in order to avoid the complications of the direct solution of the combustion wave, it is common practice to use simple empirical relations for the burning rate evaluation, for example, the largely and successfully used expression of Vieille's-de Saint Robert's law [2,8].

$$r_b = a p_c^n \quad (2)$$

### **1.7 Tail off**

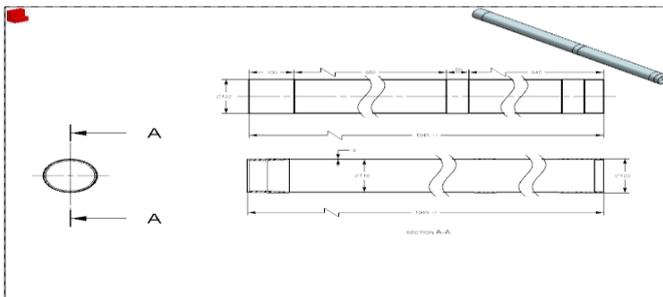
As the burning surface recedes and decreases in time, larger and larger parts of the liner and the case thermal protections are exposed to the action of the chamber hot gases. As a consequence, they are heated and because of ablative phenomena, begin to add ablation products in the chamber. As the grain combustion products mass addition into the chamber

becomes smaller and smaller, a rapid decrease of the chamber pressure occurs, and combustion actuations and sliver generation can also occur.

This operative phase is, therefore, characterized by unsteady events, related to the chamber pressure decrease in time, mixing of gases coming from the residual grain propellant combustion and case thermal protections ablations. Thus, they need to be described correctly by an accurate burning surface evolution evaluation [8].

## 2. Model description:

The Solid Rocket Motor of 122mm rocket consists of motor case (122mm diameter, total length 1945±1mm, with nozzle 2228mm), nozzle (divergent convergent), propellant grain, internal insulation and the igniter; figure (1-6).



**Figure 5: Simplified model of (SRM)**

The SRM of 122mm motor was studied. It has a relatively simple conical shape of the grain propellant and a simple cylindrical case. The propellant used in SRM of 122mm its composition and characteristics are reported in the tables below. It has a burning rate with parameter  $a = 10$  at temperature 20°C, a burning rate exponent of APN De Vieille Saint Robert of  $n = 0.3$  and a density of about 1.76 Kg/m<sup>3</sup>.

In this composite propellant, aluminum percolate (AP) is the oxidizer; HTPB is the binder, oxamide the fuel and the carbon black is used as an opacifier. The opacifier has the

function of ensuring that the heat does not penetrate far below the surface of the grain, which could cause detonation. The opacifier also prevents sub-surface overheating and localized premature ignition in the grains where imperfections absorbing the thermal radiation are present.

**Table 1: Formulation sheet**

MATERIAL CODE	SPECIFICATION	%
HTPB		8.5
MAPO		0.09
DOS		2.91
TPFE		2
TDI		0.5
AP	60-80	21.8
AP	100-140	21.5
AP	5-10	25
AL		17.2
X-585		0.5
H		0.14
Hx		0.1
Bx		1

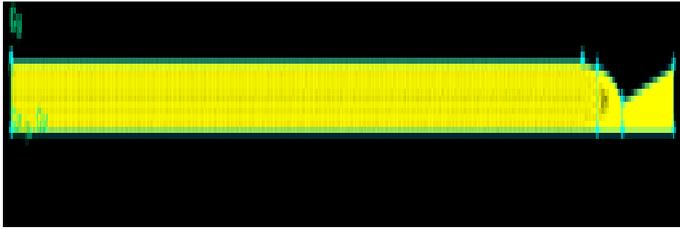
**Table 2: Mechanical properties**

PROPERTIES CODE	TENSILE MPA	EXTENSIBILITY% %	DENSITY-G/ML	HARDNESS SHERE
FR-122	0.8-1	≥35	1.760-1.800	≥50

### 3- Simulation of the model.

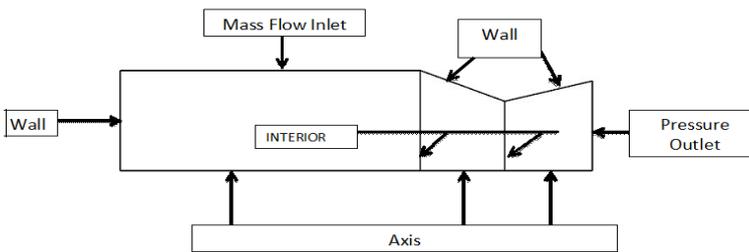
#### 3.1-ANSYS FLUENT Model preprocessing for 122 mm (SRM) steps:

1. 2D ANSYS FLUENT model of 122 mm (SRM) was prepared by NX-UG CAD software and concentrated mesh by using preprocessor Gambit 2.4.6 at exit area and nozzle as shown in figure (5).



**Figure 5: Mesh Distribution**

2- Specify Boundary Types in GAMBIT as in figure (6).



**Figure 6: Boundary condition Types**

3-To calculate burning rate of the grain which is had star shape at front and cylindrical bore shape we build program using C++ language and used User Define Function (UDF).

4-We choose  $k - \epsilon$  SST Models.

### 3.2- Post processing (simulation result).

There are several quasi-steady formulations to predict the burning rate of an energetic solid material. One of them is the APN model, which is an empirical model suitable for composite propellants in the absence of a more suitable fundamental combustion model. The APN model approximates the burning rate as solely dependent on the mean local pressure using the Vieille's or Saint Robert's law:

$$r_b = a p_c^n \quad (2)$$

Where  $p_c$  is the chamber pressure,  $a$  is an empirical constant influenced by ambient grain temperature, also known as the

temperature coefficient, and  $n$  is the burning rate exponent, or the combustion index, and it is independent of the initial grain temperature and describes the influence of chamber pressure on the burning rate.

$$r = aP^n = a_0 \bullet e^{\tau(T-T_0)} \bullet P^n \quad (3)$$

Propellant burning rate

Chamber pressure  $p_c$  (MPa)

Propellant temperature  $T$  (°C)

Referenced temperature  $T_0=20^\circ\text{C}$

Pressure exponent  $n=0.3$

Burning rate coefficient  $a$  (cm/ ((MPa)<sup>n</sup> · S))

$T_0=20^\circ\text{C}$ ,

$$a_0 = 1.001 \text{ cm} / (\text{MPa})^n \cdot \text{s}$$

$$\tau = 0.00241 / ^\circ\text{C}$$

### 3.2.1-Simulation under 20 °C:

Propellant burning rate  $r = aP^n = a_0 \bullet e^{\tau(T-T_0)} \bullet P^n$

$n=0.3$      $a = 10$      $T = 20^\circ\text{C}$

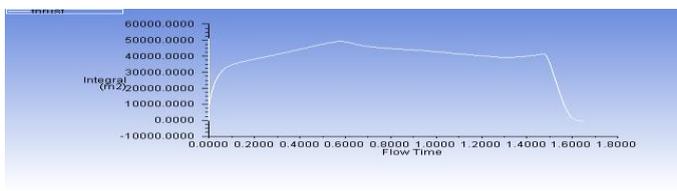


Figure 7: Thrust – Time curve (20°C)

### Contours of custom field functions

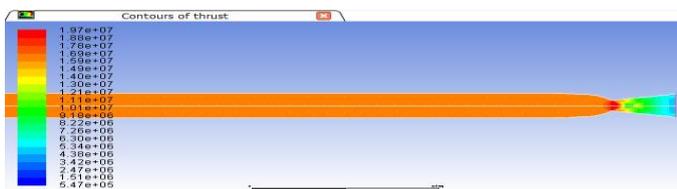


Figure 8: Contours of thrust (20°C)

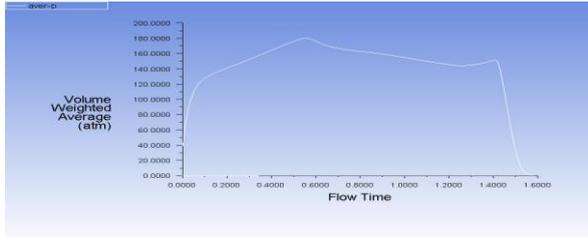


Figure 9: Pressure – Time curve (20°C)

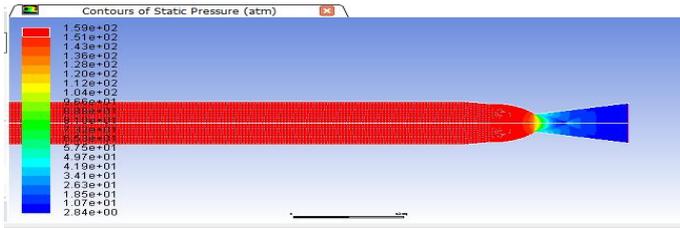


Figure 9: Contours of static pressure (20°C)

### 3.2.2 Simulation under 50°C:

Propellant burning rate  $r = aP^n = a_0 \cdot e^{\tau(T-T_0)} \cdot P^n$   
 $n=0.3 \quad a = 10.3 \quad T = 50^\circ\text{C}$

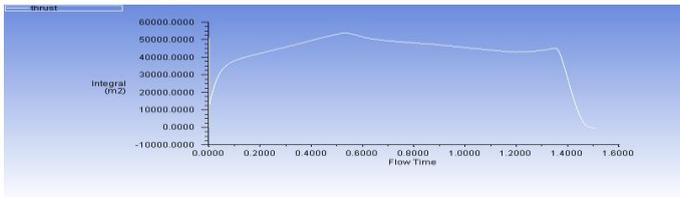


Figure 10: Thrust – Time curve (50°C)

### Contours of custom field functions

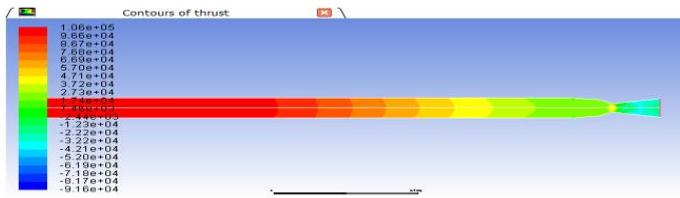


Figure 11: Contours of thrust (50°C)

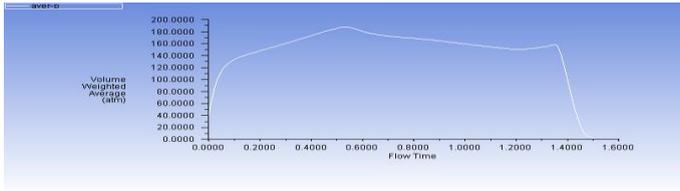


Figure 12: Pressure – Time curve (50°C)

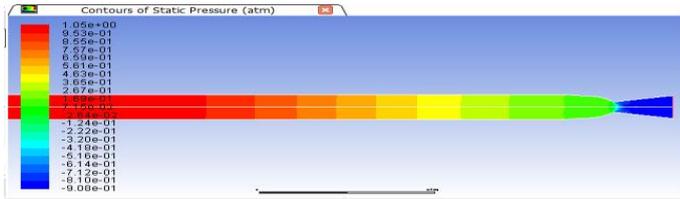


Figure 13: Contours of static pressure (50°C)

### 3.2.3 Simulation under 35°C:

Propellant burning rate  $r = aP^n = a_0 \cdot e^{\tau(T-T_0)} \cdot P^n$   
 $n=0.3 \quad a = 10.15 \quad T = 35^\circ\text{C}$

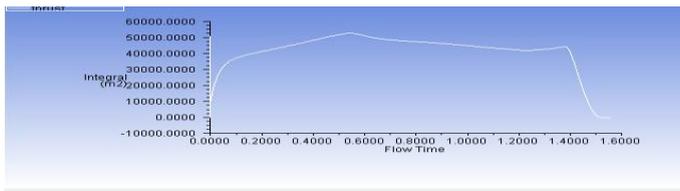


Figure 14: Thrust – Time curve (35°C)

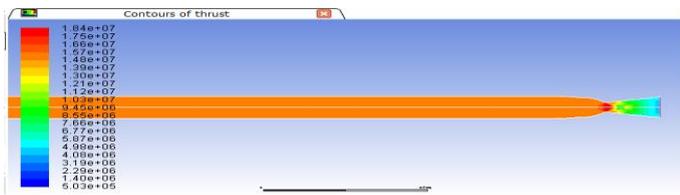


Figure 15: Contours of thrust (35°C)

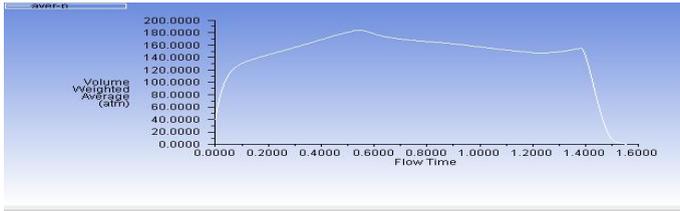


Figure 16: Pressure – Time curve (35°C)

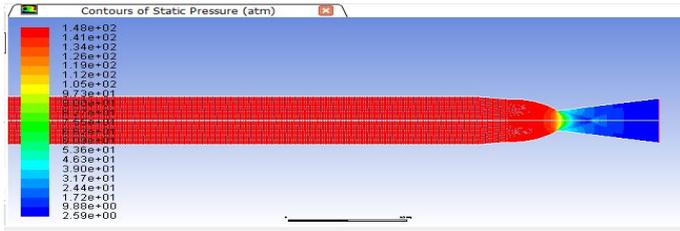


Figure 17: Contours of static pressure (35°C)

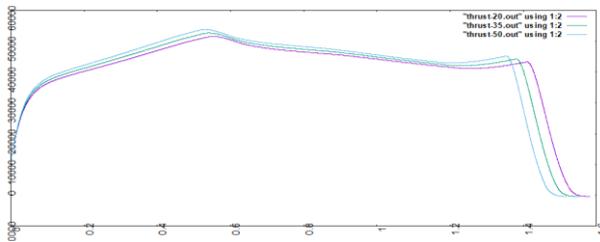


Figure 18: comparison of thrust at different temperature

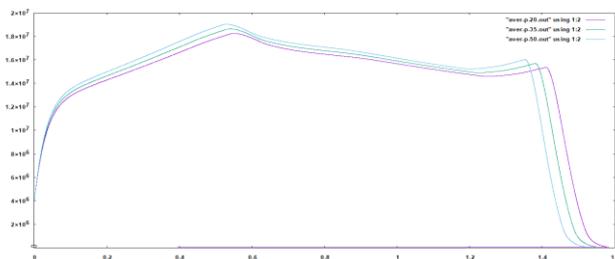


Figure 19: comparison of pressure at different temperature

## 4. Experimental Work Setting.

### 4.1 Experimental test (Ground static test station).

We fixed the 122mm (SRM) with horizon angle 0 degree by two movable fixtures on 150 mm thickness steel plate (railway). We

put the pressure sensor at the front side inside the motor case where we put thrust sensor at the front side in front of the motor near to the metal which suspending to the concrete wall. As shown in figure 17.

The ground static test station is consisting of:-

- a. Thrust sensors its maximum rang (0~50) KN.
- b. Pressure sensors it's maximum range (0~20)MPa.
- c. Control room.
- d. Data acquisition unit for analysis of data.
- e. Temperature gauge.

Implement firing static test (experimental test) for the new models (in different temperatures).



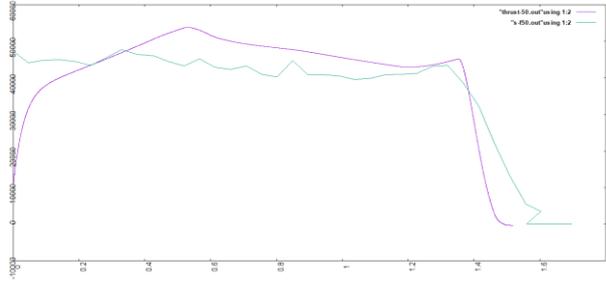
**Figure 20: Ground static Test Setting(SRM on the static test stand)**



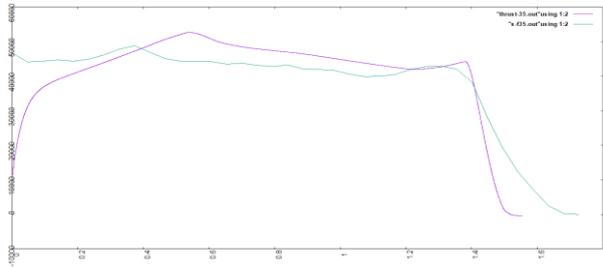
**Figure 21: Ground static Test (firing)**

## 4.2 Experimental test results and discussion

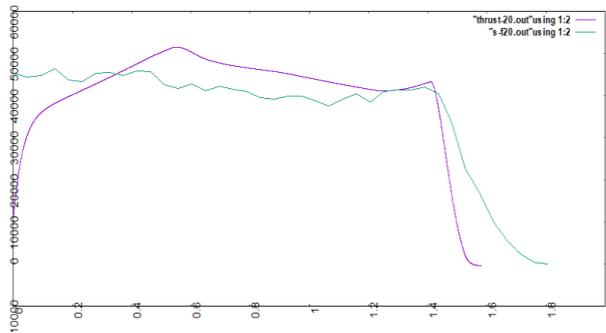
### 4.2.2 Thrust results:



**Figure 22: Thrust at 50°C**



**Figure 23: Thrust at 35°C**



**Figure 24: Thrust at 20°C**

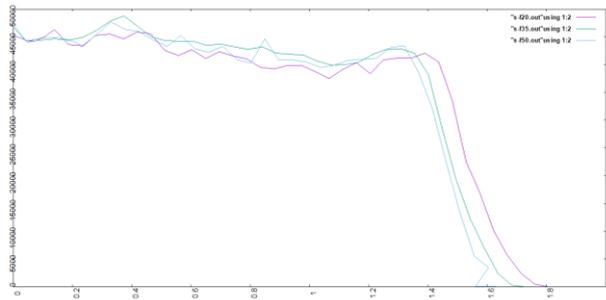


Figure 25: Comparison thrust at different temperatures (20,35,50) °C

### 4.2.3 Pressure result

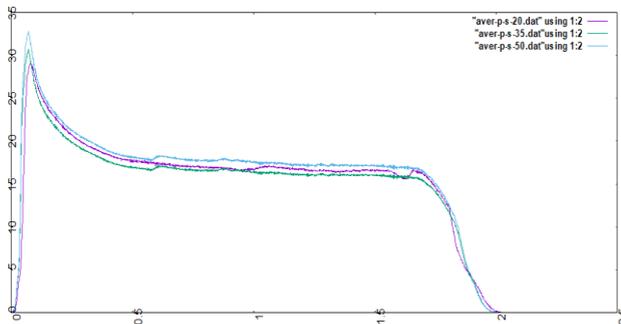


Figure 26: Comparison pressure at different temperatures (20,35,50) °C

## 5. RESULT & DISCUSSION

Table 3: results from thrust and pressure time curve at different temperature

S	Temperature (°C)	Parameters						Thrust deviation % (simulation & experimental)	pressure deviation % (simulation & experimental)
		Burning rate coefficient (a) (cm/((MPa) <sup>0.5</sup> s))	Burning Time duration (second)						
			simulation		Experimental				
			Thrust curve	Pressure curve	Thrust curve	Pressure curve			
1	20	10.00	1.5837	1.5853	1.67821	2.0269	5.6	21.8	
2	35	10.15	1.5402	1.5555	1.61122	2.0030	4.4	22.3	
3	50	10.30	1.5182	1.5283	1.57105	1.9978	3.4	23.5	

From table 3:

1-We can see that the temperature had reverse proportion with the thrust burning time and also with pressure burning time at simulation and experimental test.

2-The Burning rate coefficient had reverse proportion with the thrust burning time and also with pressure burning time at simulation and experimental test.

3-The deviation of thrust time and pressure time between simulation and experimental is acceptable.

**Table 4: Tail off stage results from thrust and pressure time curve at different temperature.**

S	Temp eratur e (°C)	Parameters						deviation % (simulation & experimental)			
		Burning rate coefficie nt (a) (cm/ (MPa) <sup>n</sup> ·S)	Tail off stage								
			simulation			Experimental					
			Start time (s)	Thrust curve	Pressure curve	Start time (s)	Thrust curve	Pressure curve	time	Thru st	Press ure
1	20	10.00	1.41	43181.1	$1.57096e^{+007}$	1.39	41965.6	$1.54041e^{+007}$	1.43	2.88	1.9
2	35	10.15	1.38	44011.7	$1.53139e^{+007}$	1.34	42871.0	$1.51325e^{+007}$	2.98	2.66	1.3
3	50	10.30	1.35	45315.7	$1.50393e^{+007}$	1.31	43449.5	$1.47301e^{+007}$	3.05	4.30	2.1

From table 4:

1-We can see that the temperature and burning rate coefficient had reverse proportion with the thrust curve and also with pressure curve at simulation and experimental test.

2-The temperature and burning rate coefficient had reverse proportion with the start time of tail off stage and also with pressure burning time at simulation and experimental test.

3-The deviation of thrust time curve and pressure time curve between simulations and experimental is acceptable.

## **CONCLUSION**

In this work we used 2D ANSYS FLUENT simulation to simulate the internal ballistic for 122mm (SRM).

The results about the internal ballistic (SRM) (thrust & pressure) between simulation and experimental show good results and was much closed, so we can use ANSYS FLUENT to simulate other different parameters.

Analytical method and Software simulation can integrate to design (SRM) and solve many kinds of problem because it's very economic and safe and faster than experimental tests.

The use of CFD allowed resolution of a much greater level of detail than could have been determined with the experimental results alone. A thorough understanding of the experimental setup and its limitations were acquired which will help in future test design and analysis.' CFD tools and techniques developed during this effort can aid in prediction of hot gas behavior in narrow solid rocket motor joints.

The benefit of the simulation will be plan to get the performance of motor and to compare the results with testing data and to validate the design data with the testing data , and the results will be an important for technical decision for establishing production lines.

### **Acknowledgments**

The authors of this paper are grateful to School of Mechanical Engineering, Sudan University of Science & Technology (SUST) for their help and support. Also they would like to express their gratitude to SMT for their continual help, guidance, and detective work during this analysis effort and test facilities and analytical .

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