

Study Heftiness in the Astrophysical Turbulence at Pakistan Air Space

KHUSRO MIAN

FAST, National University of Emerging Sciences
Main Campus, Karachi, Pakistan
Institute of Space & Planetary Astrophysics
University of Karachi, Karachi, Pakistan.

S. ZEESHAN ABBAS¹

Department of Physics
University of Karachi, Karachi, Pakistan

MOHIB R KAZIMI

Department of Applied Chemistry & Chemical Technology
University of Karachi, Karachi, Pakistan

FAYYAZ UR RASHEED

Institute of Space & Planetary Astrophysics
University of Karachi, Karachi, Pakistan

ALAY RAZA

SHEIKH M. ZEESHAN IQBAL

Department of Physics
University of Karachi, Karachi, Pakistan

Abstract:

The fundamental assignment of statistical astrophysics is to study macroscopic phenomena that result from microscopic interaction among many entity components. This problem is similar to many investigations undertaken in space plasma. In particular, open system under nonlinear regulation, such as unperturbed electron concentration is a good candidate for such an approach, Therefore, it seems reasonable to consider the possibility that dynamical systems under concentration may exhibit temporal structures which are similar, under certain conditions, to those found in physical systems. Indeed, concepts and techniques originating in statistical astrophysics are showing promise as useful tools for quantitative analysis of complicated nonlinear systems.

¹ Corresponding author: szabbas@uok.edu.pk

In this communication we study the Robustness in the ionospheric turbulence: a case study at Pakistan ionospheric region. Robust method is powerful tool to increase accuracy and reliability of statistical modeling and data analysis. Using Robust / Resistant Estimates location can be obtained by making average less sensitive to outliers. Trimmed mean \bar{x} and variance σ^2 calculations are discussed of ionospheric turbulence data. The information attained from these analyses to vary possible parameters and variables in the physical system to realize an optimal performance.

Key words: Robust, Resistant, Turbulence, Ionospheric, Outliers, Trimmed.

Introduction

The pulse sounding technique of Breit and Tuve (1925) is still a basic tool of ionospheric research. A sounder is a type of radar which is capable of obtaining echoes from the ionosphere over a wide range of operating frequencies. In the E and F regions, the collisions are sufficiently infrequent that for many purposes such as ionosonde measurements of electron concentration. Its imaginary part is related to the absorption coefficient, in which the positive and negative signs apply to the ordinary and extraordinary mode, respectively; the angular frequency of the radio wave; and the real part of the refractive index derived from the Appleton Hartree. The absorption of radio waves has been used as a means of investigating the ionosphere.

Atmospheric variables such as parcel velocity, virtual height, critical frequency plasma concentration, plasma frequency of F2 layer of ionosphere, also their perturbation quantities of there parameters. Show both chronological and spatial fluctuation on the other hand, in general considerable mode of uniqueness is there between our comments of these quantities. Take either at the same location like Pakistan regions alienated by short chronological section; or at the same

time dissimilar site [1]. In arrange to portray such variables in a sensible way, it is necessary to think probabilistic approach that permit for both variability reliance [2,3]. Such approaches are helpful for characterizing atmosphere processes such as quantifying the plasma turbulence for ionospheric F2-layer at Pakistan air space (PAS) in term of complete parameters. Also it is essential to make result about atmosphere F2-layer ionosphere plasma.

We present some probabilistic approaches that establish claim in atmosphere science the plasma turbulence for ionospheric Es-layer at Pakistan air space. To inferences about these reliant atmosphere comments, the probability theory stochastic processes will be careful. Quantify the plasma turbulence for ionospheric data F2-layer at Pakistan air space we perform EDA that is now being incorporated into formal statistical theory. It will provide a comprehensive characterization of underlying system in the form of mathematical models. The information attained from such analysis can be further employed to very possible parameters and variable in the system to achieve an optimal performance. One such statistical approach is well within the feasibility and approach of the available computational software that rely on graphical techniques such as histogram, probability plot, P-P plot, and Q-Q plot [4-9].

Analysis Data:

- (a) Regarding the quantify the plasma turbulence for ionospheric F2-layer at Pakistan and the conforming histogram we mention to Figure. 1. The design means the likelihood of apiece worth of the plasma turbulence.

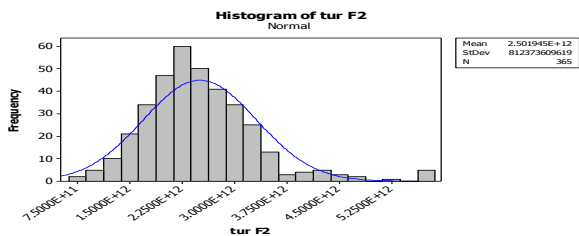


Fig. 1: Histogram of numerous numbers of comments of plasma turbulence.

(b) The part beneath the flat line section at a specific plasma turbulence signifies the likelihood of apiece worth of the plasma turbulence. Figure 2 represents the Normal distribution for plasma turbulence for the overhead thought retro.

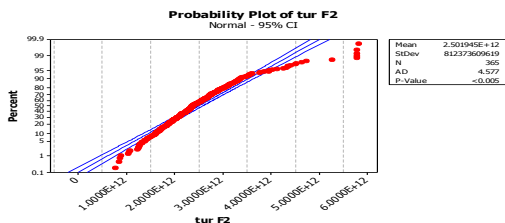


Fig.2: Gaussian Function for plasma turbulence at ionospheric F2-layer

(c) For Gaussian data, the example nasty and alteration are the unbiased estimators of location of the Gaussian distribution. Greatest bodily information circles are not Gaussian distributed smooth after alteration, since the supposition of Gaussian distribution is a exact romanticism that is not ever encountered precisely in repetition since big data groups unavoidably cover outliers [10].

(d) Anderson-Darling Normality Test

Robust estimates for site can be got by creation the mathematics nasty less subtle to outliers. In fact it is slim a

amount of the information from apiece culmination of the well-ordered information usual and then to calculate the nasty of the residual standards (Murphy and Richard 1985). These clipped income from a domestic of estimators that can be indexed by α , the portion of comments clipped at each end of example. Approximations that are not excessively prejudiced by a minor amount of outliers are called resilient [11-13].

Table-1; Analysis of Plasma Turbulence

Statistics	Result Values
Observation	0365
A-Squared	4.570
P-Value <	0.0050
Mean	2.501960x10 ¹²
St.Dev.	8.126670x10 ¹¹
Variance	6.604270x10 ²³
Skewness	1.220630
Kurtosis	3.067160
Median	2.392760x10 ¹²
Q1	1.973520x10 ¹²
Q3	2.896970x10 ¹²
Min Observation	7.822490x10 ¹¹
Max Observation	5.825680x10 ¹²

- 95% Confidence Interval for Mean
2418313593546 2.58561x10¹²
- 95% Confidence Interval for Median
2330558649780 2.49808x10¹²
- 95% Confidence Interval for St. Dev
757679247089 8.76326x10¹¹

Robust Estimates for Location

One of the simplest ways of making arithmetic mean less sensitive to outliers is to droplet “fit” a amount of the information from each end of the well-ordered data set and then to calculate mean of the residual values [14]. These clipped

means form a domestic of estimators that can be indexed by α , if $x_1 \leq x_2 \leq x_3 \leq \dots \leq x_n$ are ordered data of a random sample of size n,

$$\bar{x} = \frac{1}{n(1-2\alpha)} \left\{ \sum_{i=k+2}^{n-k-1} x_i + (1+k-n\alpha)[x_{k+1} + x_{n-k}] \right\}, \text{ if } k+2 \leq n-k-1$$

Otherwise,

$$\bar{x} = \frac{1}{2} [x_{k+1} + x_{n-k}].$$

Here k is the largest integer less than or equal to $n\alpha$ or $0 < \alpha < 0.50$.

If $n = 365$, $\alpha = 0.050$

Robust Mean = 2.45×10^{12}

Robust Estimates of Scale

The estimation of advanced instruction instants such as alteration includes resolution of a battle of attention, meanwhile one would similar to defend the approximations from outliers, nonetheless knows that the approximation of advanced instruction instants trusts additional deeply on data in the ends of the delivery. Therefore, a sure quantity of carefulness in consuming robust estimates of the alteration is designated. Well minor data sets, the forecaster may be well off by learning the examples actual prudently and lone neglecting obviously designates outliers [15,16].

Trimmed Variance

The thoughts Gaussian clipped means can also be practical to the approximation of the alteration. The clipped alteration is distinct as

$$s_{\alpha}^2 = \frac{c_{\alpha}}{n(1-2\alpha)} \left\{ \sum_{i=k+2}^{n-k-1} [x_i - \bar{x}_{\beta}]^2 + (1+k-n\alpha) \{ [x_{k+1} - \bar{x}_{\beta}]^2 + [x_{n-k} - \bar{x}_{\beta}]^2 \} \right\}$$

where \bar{x}_{β} is a robust estimate of location generally a β -trimmed mean with $\beta = \alpha$, c_{α} is a normalizing constant to brand the clipped alteration an impartial approximation of the alteration under sure circumstances, and k is the largest integer less than or equal to $n\alpha$.

C alpha are founded on instants of instruction statistics of the Gaussian distribution, and indirectly shoulder that the “central” of the data is sensibly standard. For big examples, C alpha can be approximated by a certain integral over the standard distribution when $\alpha = 0.050$ and n is big, C alpha = 1.605. Because of the reason just outlined, it is usually advisable to use somewhat smaller trimming properties for variance estimate than for location.

$$\begin{aligned} \text{Robust Variance (or Trimmed Variance)} S^2 &= 8.26 \times 10^{22} \\ S &= 2.874021573 \times 10^{11} \end{aligned}$$

The Inter quartile Range

Additional robust amount of scale, which is equivalent to mean absolute deviation as distant as simplicity of calculation and little competences under the close standard assumption, is the IQR.

IQR = upper quartile – lower quartile.

For symmetric data **MAD=IQR/2**, for non-symmetric data, working with for inter quartile range has the advantage that, once the quartiles and the median are computed, the differences higher quartile medium and median lower quartile give us some clues about the symmetry of the data. Furthermore, the IQR has a actually agreeable real clarification

it is the range within which the central of the information lie) and can be straight connected to the box plot.

The asymptotic worth for the standardization continuous C_{IQ} underneath the assumption of ordinariness in the central of the data is 1.35, so that

$$S_{IQ} = IQ / C_{IQ}$$

The actual value of these normalization constants is, of course, unimportant if the scales of several sets of information are likened, since lone the comparative sizes are of importance.

Median Absolute Deviation (MAD)

The gage approximate that is the complement of the middle as the greatest resilient estimator for site is the MAD from the middle; that is, $MAD = \text{median} |x_j - \text{median}(x_i)|$.

$$1 \leq j \leq n \qquad 1 \leq i \leq n$$

MAD has to be separated by a regularizing continuous C_{MAD} to brand it a error free guesstimate of the St. Dev. and the problems discussed for the regularizing coefficients of clipped alterations apply here as well. In the usual circumstance, the asymptotic worth of C_{MAD} for n treatment to eternity 0.6745, therefore we define the gage estimate

$$S_{MAD} = \frac{MAD}{C_{MAD}}$$

The asymptotic efficiency of the MAD-estimate for normal data is very low. On the other hand, it is actual informal to calculate. AD can thus be regarded as a crude, nonetheless humble and harmless, scale estimate. It can be used, while no advanced accuracy is essential, as a humble checkered on additional complication computations or as a starting point for iterative procedures.

It is valuable because of its ease of the calculation and little competences.

We have plasma turbulence data from Table-1 $n= 365$, median = 2.39276×10^{12} , lower Quartile = 1.97352×10^{12} , upper Quartile = 2.89697×10^{12} so

$$\text{Upper MAD} = 5.0421 \times 10^{11}$$

$$\text{Lower MAD} = 4.1924 \times 10^{11}$$

$$\text{IQ} = 9.2345 \times 10^{11}$$

For the symmetric case AD can be calculated as $\text{MAD} = \text{IQR}/2$

$$\text{MAD} = 4.61725 \times 10^{11}$$

$$S_{\text{MAD}} = 6.8914179 \times 10^{11}$$

$$S_{\text{IQ}} = 6.84541067 \times 10^{11}$$

$$S = 2.874021573 \times 10^{11}$$

Analyzing information in this method is one of the main requests of robust / resistant approaches (Buggi, 1996).

Conclusion:

Communication by electrical means began in 1844 after this system were being developed the theoretical foundation for electromagnetic radiation was being laid by Maxwell. The means of astrophysical plasma turbulence astrophysics is a branch of astronomy, plasma is a quasinutral gas have collective behavior, turbulence is an exciting state due to solar radiation. The finite resistance in the plasma results in joule heating of the gas, causing temperature 10^7K . The astrophysics plasma turbulence that is the serious threat to our communication is consisting of active ionosphere. The major terrestrial effects include radio wave propagation, danger for small satellite communication, rocket and missile technology. The more common phenomena affecting the propagation of electromagnetic waves and the influence this effect has on the performance of a communication system.

There are two communication system non electromagnetic and electromagnetic radiations. Such non electromagnetic radiation will introduce an attenuation of

around 2 to 3 dB/Km at frequency around 10 kHz and loss is around 4 to 5 dB/Km. a fundamental characteristic of non-electromagnetic radiation is that the attenuation is exponential in its behavior. Using electromagnetic radiation, the signal power is radiated into a substantial angular region of space by the transmitting device and only a small fraction of this radiated power is intercepted by the receiving device. There is thus a very significant coupling loss between the transmitting and receiving devices. The loss incurred versus distance is algebraic in behavior rather than exponential. For a lot of communication links as the radiated power per unit area incident on the receiving device decreases as the inverse square of the distance between the transmitting and receiving devices.

In this statement we have labelled bodily conduct of plasma turbulence for ionospheric F2 layer at Pakistan air space. Using this analysis Robust / Resistant Estimates, Probabilistic and the mean absolute deviation models are established to revision the plasma turbulence. These models provided a complete account of the procedure. This method is fine clarified within the probability of computational examination that along with their corporeal clarifications are very valuable for civic and isolated sector organizations.

Acknowledgement

The authors of this paper pay their gratitude to the technical staff of SUPARCO at Karachi station, for providing DGS-256 Data used in this communication.

REFERENCE

- [1] Karl Johan Astrom Bjorn Wittenmark, Adaptive Control 2nd Ed., Pearson Education Singapore Pte. Ltd., India, 2003.
- [2] Daniel S. Yates, David, S. Moar and George P. Mc Cabe, The Practice of Statistics, W.H. Freeman and company, New York, 1996.

- [3] Allan H. Murphy and Richard W. Katz, Probability, Statistics, and decision Making in the Atmospheric Sciences, Westview Press, Ine. Boulder and London, 1985.
- [4] Fred Caswell, Helen Wright Success in Statistics, John Murray (Publishers) Ltd. London, 1982.
- [5] P.N.ARORA, SUMEET ARRORA, Mrs. S. ARROA, Comprehensive Statistical Methods, S. Chand & Company Ltd. Ram Nagar, New Delhi, 2007.
- [6] P. V. Rao, Statistical Research Methods in the Life Sciences, Brooks / Cole Publishing Company USA, 1998.
- [7] Ricardo A. Maronna, R. Douglas Martin and Victor J. Yohai, Robust Statistics Theory and Methods, John Wiley & Sons Ltd, The Atrium, Southern Gate, Chichester, West Sussex PO19 8SQ, England, 2006.
- [8] Chen M.C, Introduction to Plasma Physics, Plenum Publishing Corporation New York, 1929.
- [9] John H. Seinfeld, Spyros N. Pandis "Atmospheric Chemistry and Physics" (From Air Pollution to Climate Change) 2nd Ed., John Wiley & Sons, Inc., Hoboken, New Jersey, 2006.
- [10] Mark Z. Jacobson, "Fundamentals of Atmospheric Modeling "IST Published, Cambridge University Press USA, 1999.
- [11] Das A C, Space Plasma Physics: An Introduction, Narosa Publishing House, 2004.
- [12] H Rishbeth, Introduction to Ionospheric Physics, Academic Press New York and London, 1969.
- [13] Arora, Sumeet Arora P. N., Comprehensive Statistics Methods, S. Chand & Comp. Ltd., New Delhi, India, 2000.
- [14] Mark Z. Jacobson, Fundamentals of Atmospheric Modeling, Cambridge University Press, USA, 1999.
- [15] Dr. TK Bandhopadhyay, Antenna Engineering, Radio wave propagation and noise, khanna publisher New Deli India, 2003, pp 23-33.

Khusro Mian, S. Zeeshan Abbas, Mohib R Kazimi, Fayyaz Ur Rasheed, Alay Raza, Sheikh M. Zeeshan Iqbal- **Study Heftiness in the Astrophysical Turbulence at Pakistan Air Space**

[16] G S N Raju, *Antenna and Wave Propagation*, , Pearson education New Deli India, 2000, pp 223-300.